

$$\underline{e^{ix} = \cos x + i \sin x}$$

$$\underline{e^{i\pi} = -1}$$

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - + \dots$$

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - + \dots$$

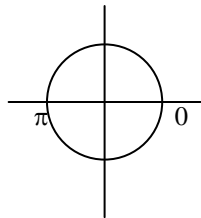
$$i \sin x = ix - \frac{ix^3}{3!} + \frac{ix^5}{5!} - + \dots$$

$$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

$$e^{ix} = 1 + (ix) + \frac{(ix)^2}{2!} + \frac{(ix)^3}{3!} + \dots$$

$$\therefore e^{ix} = 1 + ix - \frac{x^2}{2!} - \frac{ix^3}{3!} + \dots$$

$$\therefore e^{ix} = \cos x + i \sin x$$



$$\cos \pi = -1$$

$$\sin \pi = 0$$

$$e^{i\pi} = \cos \pi + i \sin \pi = -1 + 0$$

$$e^{i\pi} = -1$$

$$i\pi = \ln(-1)$$